

Quantum: Introduction, Concepts, and Applications

Luis Mendoza, PhD

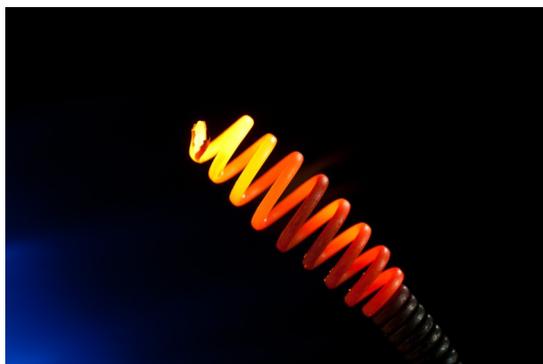
What is quantum?

- Fundamental physics theory that describes atoms and subatomic particles
- Developed early 20th century, to explain:

What is quantum?

- Fundamental physics theory that describes atoms and subatomic particles
- Developed early 20th century, to explain:

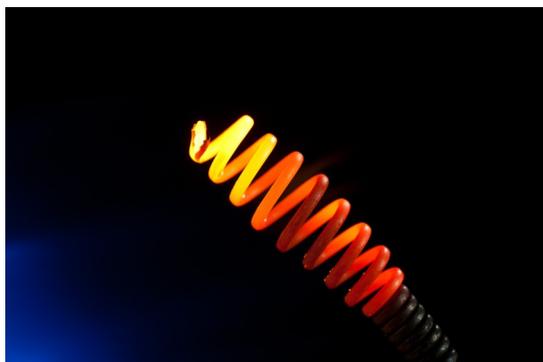
Black-body radiation



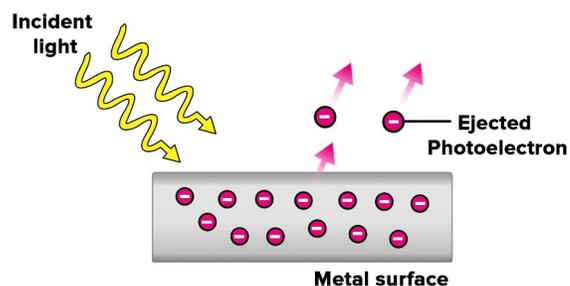
What is quantum?

- Fundamental physics theory that describes atoms and subatomic particles
- Developed early 20th century, to explain:

Black-body radiation



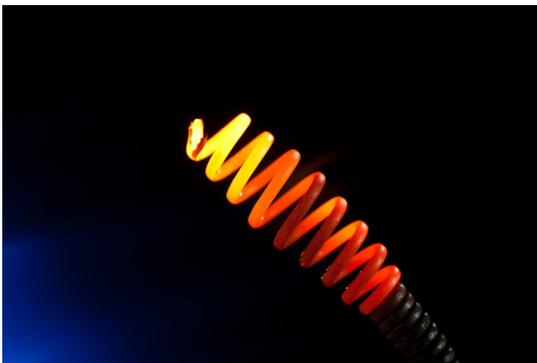
Photoelectric Effect



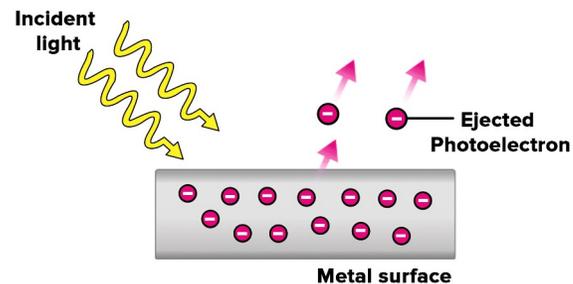
What is quantum?

- Fundamental physics theory that describes atoms and subatomic particles
- Developed early 20th century, to explain:

Black-body radiation

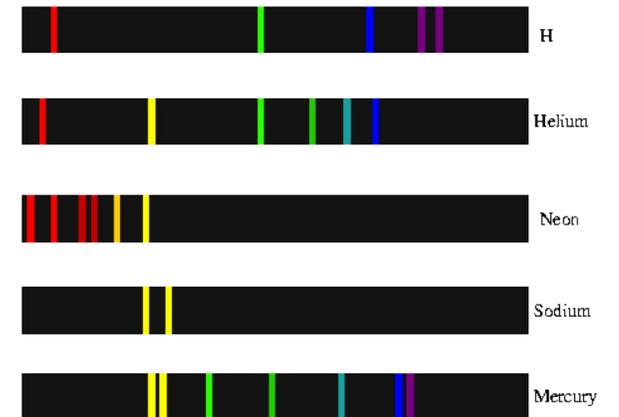


Photoelectric Effect



And many more...

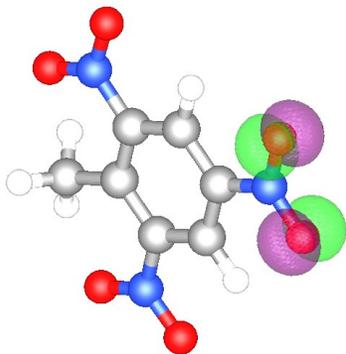
Atomic Spectra



What is quantum?

- Very different from classical physics!
- Counter-intuitive but also very useful!
- Has impacted several fields:

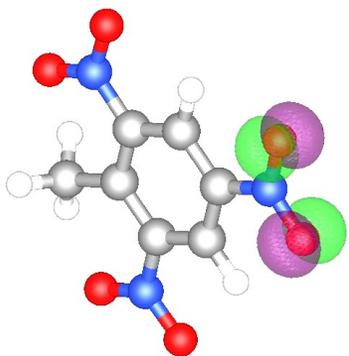
Chemistry



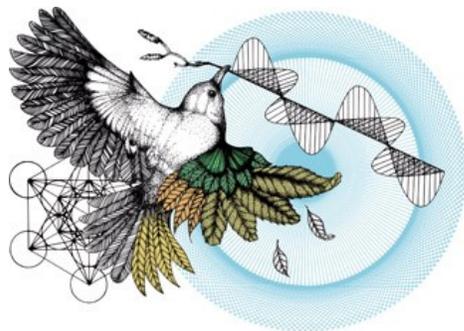
What is quantum?

- Very different from classical physics!
- Counter-intuitive but also very useful!
- Has impacted several fields:

Chemistry



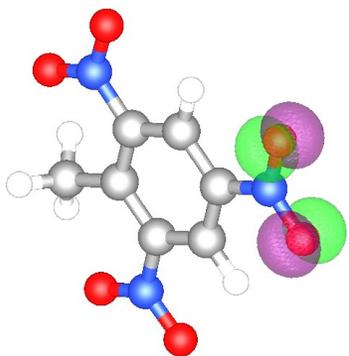
Biology



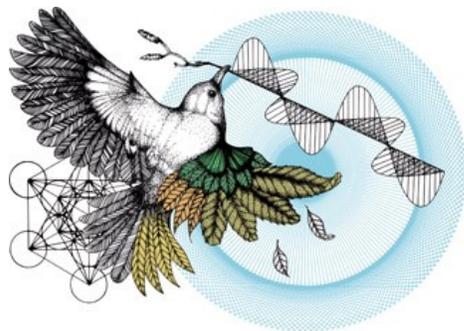
What is quantum?

- Very different from classical physics!
- Counter-intuitive but also very useful!
- Has impacted several fields:

Chemistry



Biology



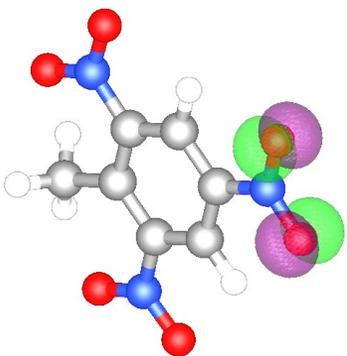
Computing



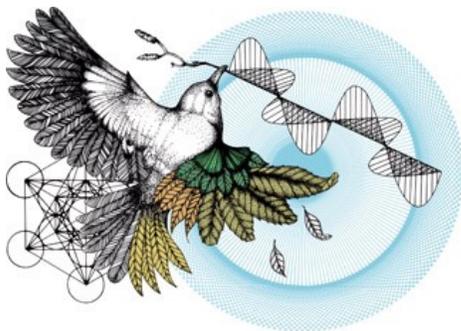
What is quantum?

- Very different from classical physics!
- Counter-intuitive but also very useful!
- Has impacted several fields:

Chemistry



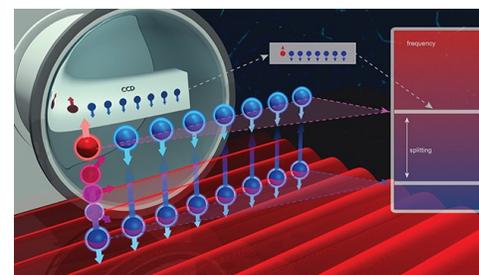
Biology



Computing



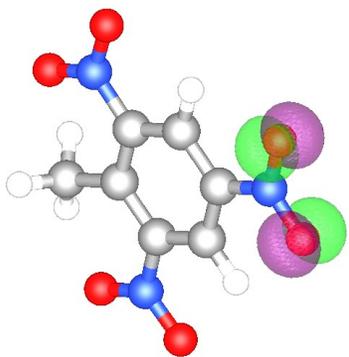
Medicine



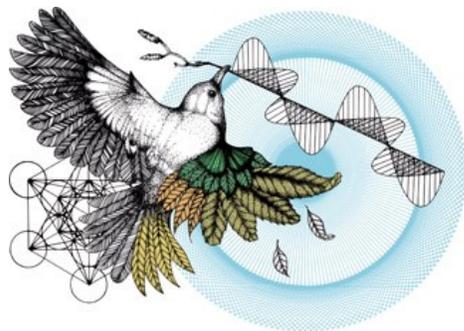
What is quantum?

- Very different from classical physics!
- Counter-intuitive but also very useful!
- Has impacted several fields:

Chemistry



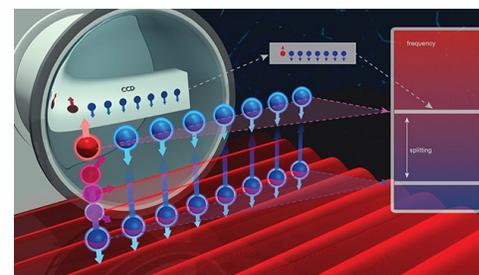
Biology



Computing



Medicine



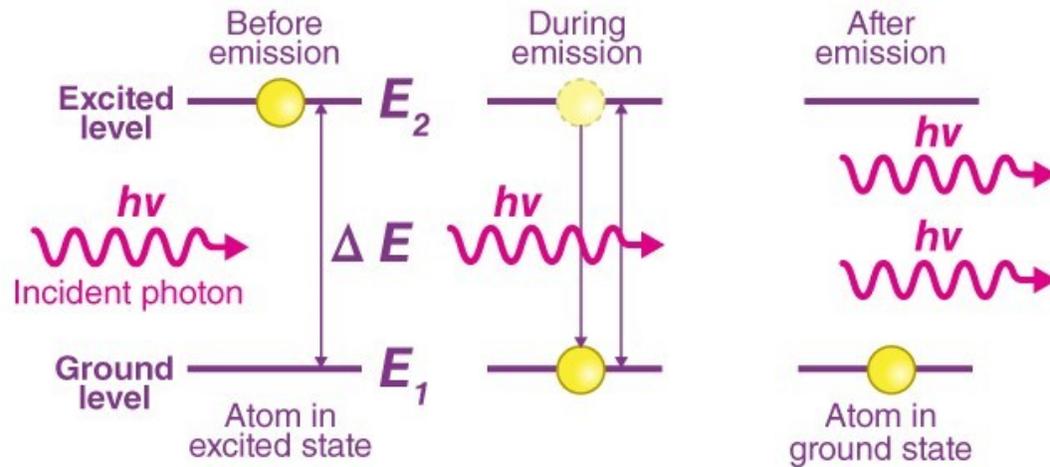
Engineering



Particle-Wave Duality

- At the quantum level particles (like electrons) can behave as waves, and waves (like light) can behave as particles

Light as particles

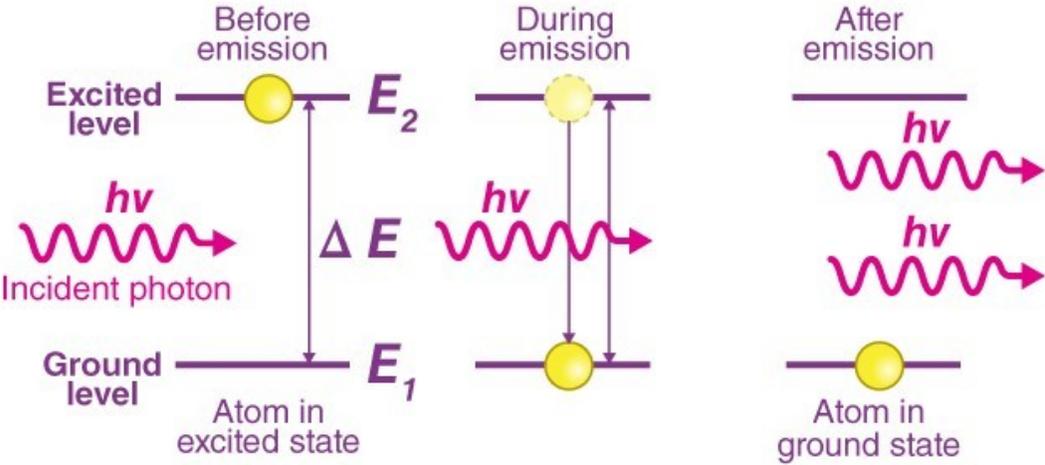


Atomic transitions

Particle-Wave Duality

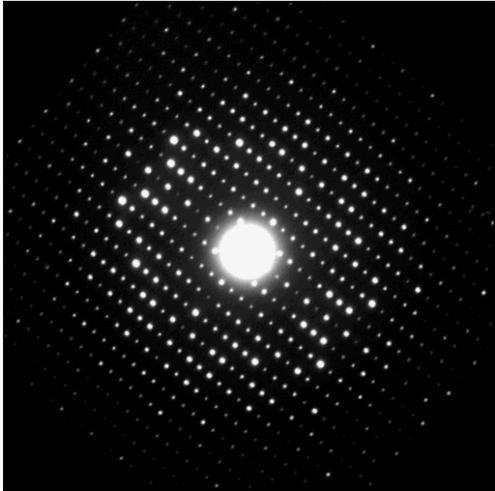
- At the quantum level particles (like electrons) can behave as waves, and waves (like light) can behave as particles

Light as particles



Atomic transitions

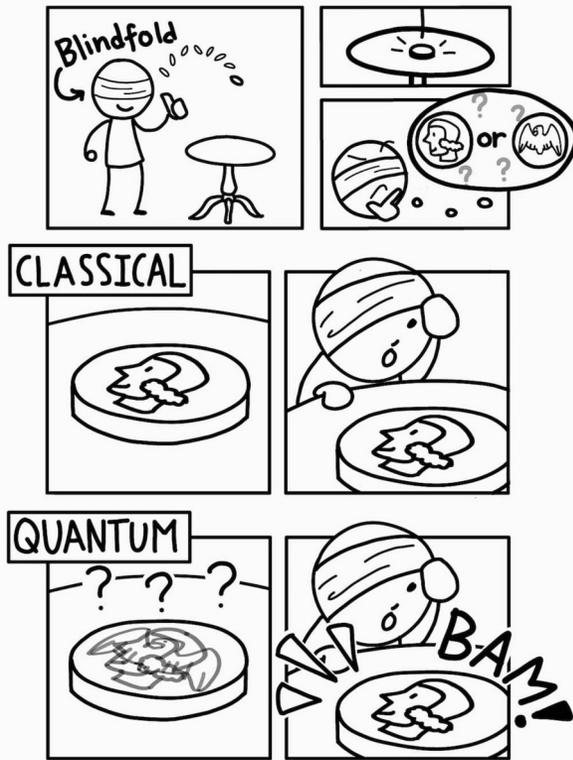
Particles as waves



Electron diffraction

Superposition

- Most quantum systems live in a superposition of many states

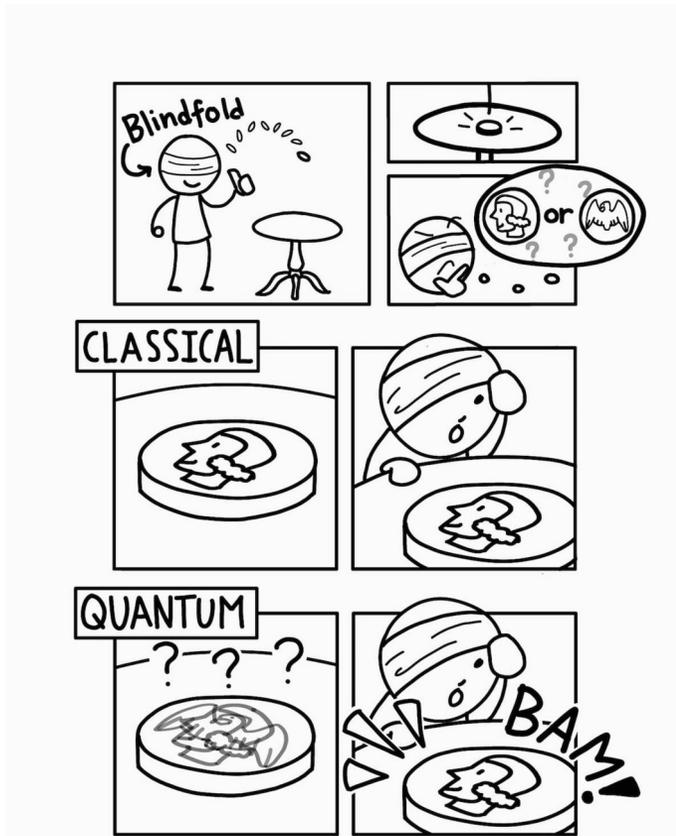


Directly observing the system has many different outcomes

Direct observations don't have a definite result,
only different results with different probabilities

Superposition

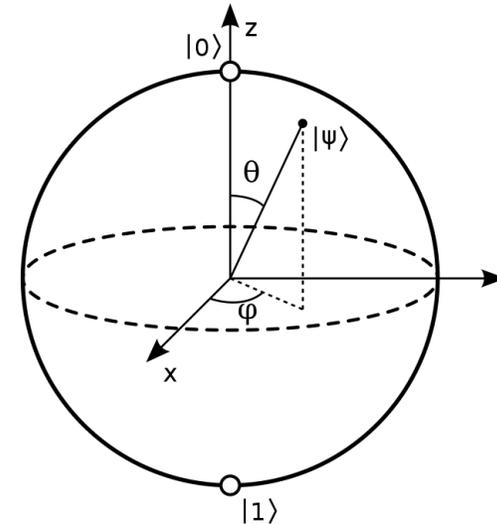
- Most quantum systems live in a superposition of many states



Directly observing the system has many different outcomes

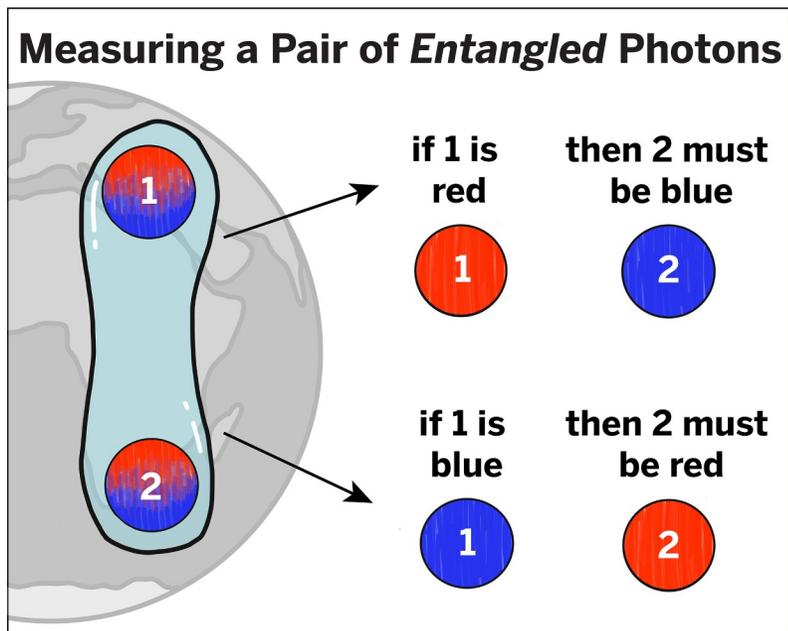
Direct observations don't have a definite result, only different results with different probabilities

Scientists use the Bloch sphere to visualize these superpositions



Entanglement

- Sometimes, quantum particles can become connected in a certain way and start behaving as a single system. This is known as entanglement



Entangled particles know each other's state no matter how separated they are

If you observe a certain property of one particle, then you will know exactly the value of that property for the second particle

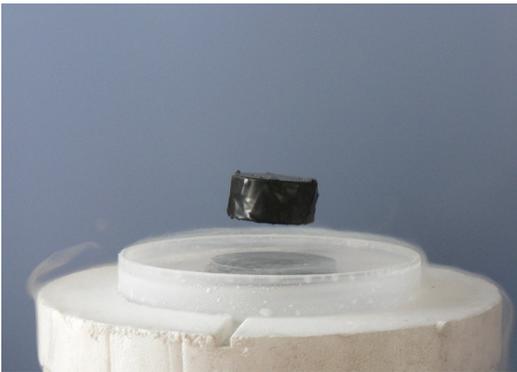
Quantum Materials

- Quantum effects only appear at subatomic sizes, but in certain situations they can have macroscopic effects!

Quantum Materials



Superconductors

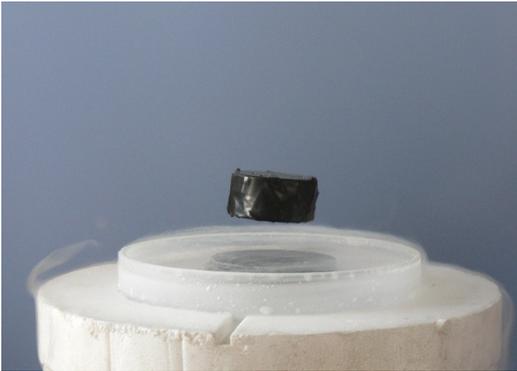


Quantum Materials

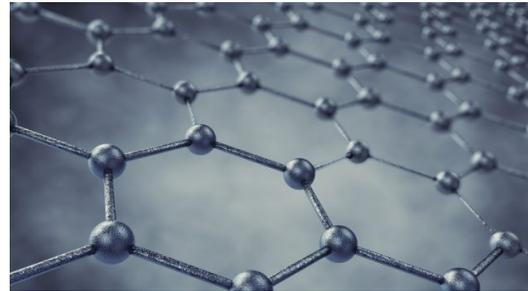
- Quantum effects only appear at subatomic sizes, but in certain situations they can have macroscopic effects!

Quantum Materials

Superconductors

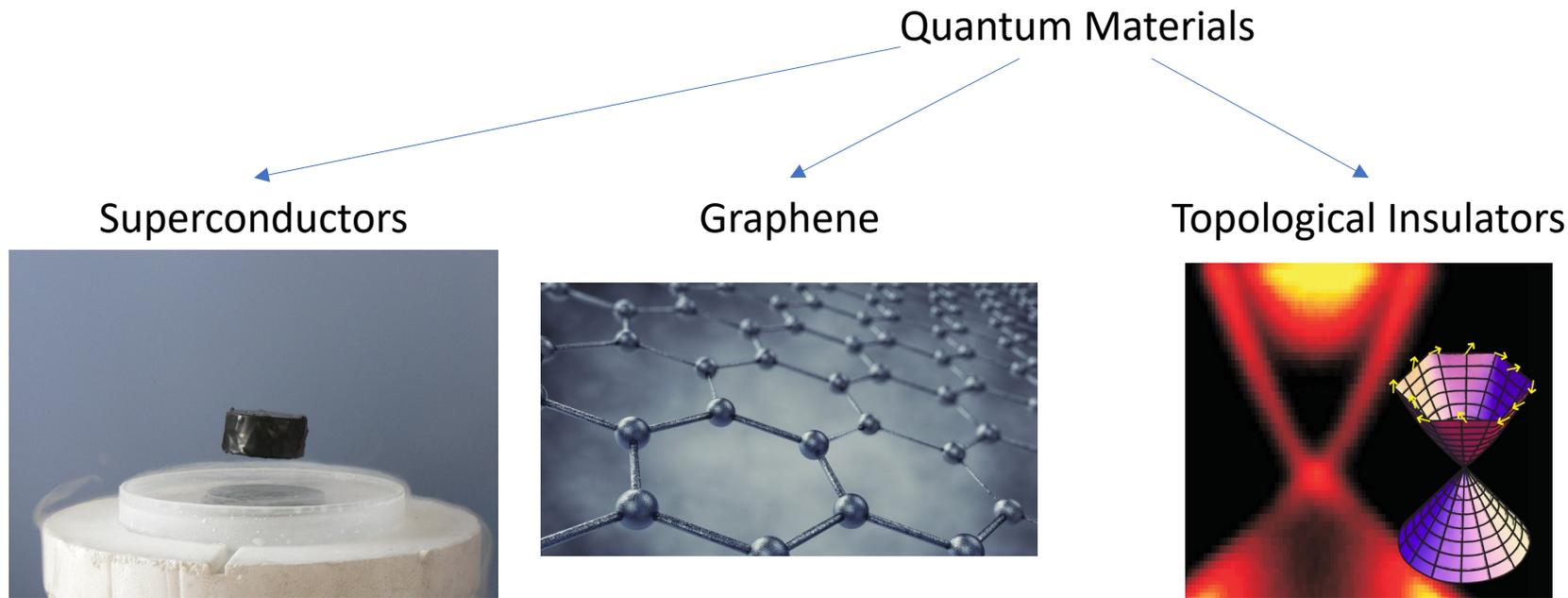


Graphene



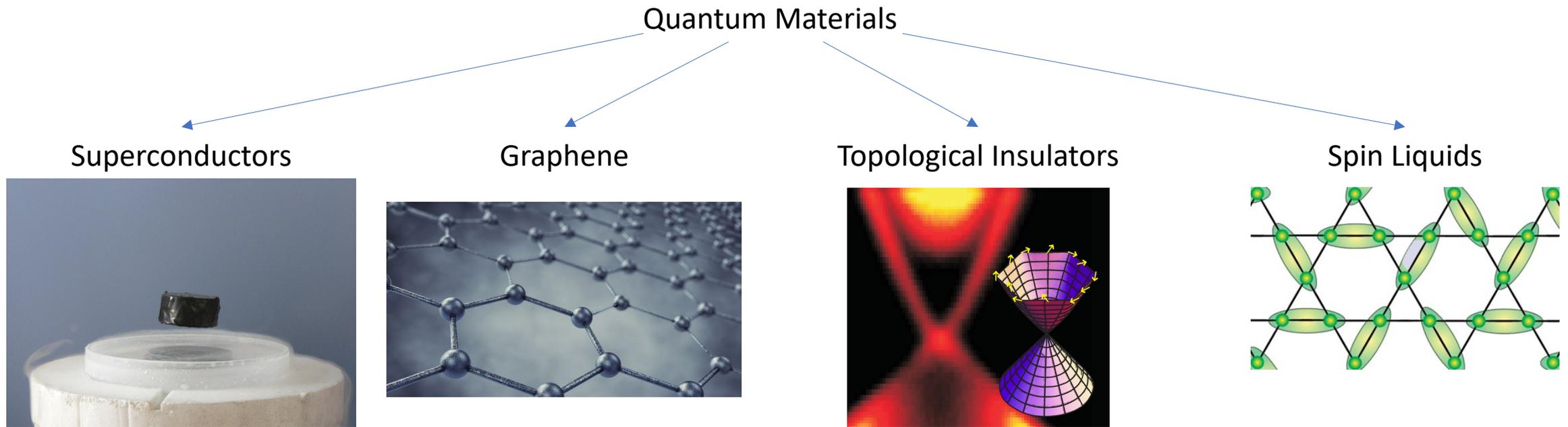
Quantum Materials

- Quantum effects only appear at subatomic sizes, but in certain situations they can have macroscopic effects!



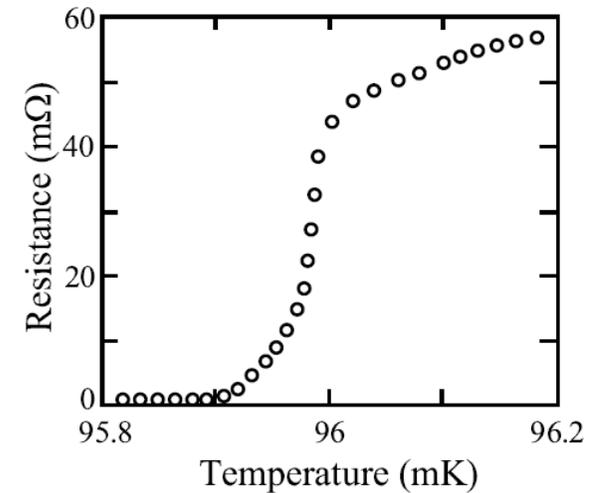
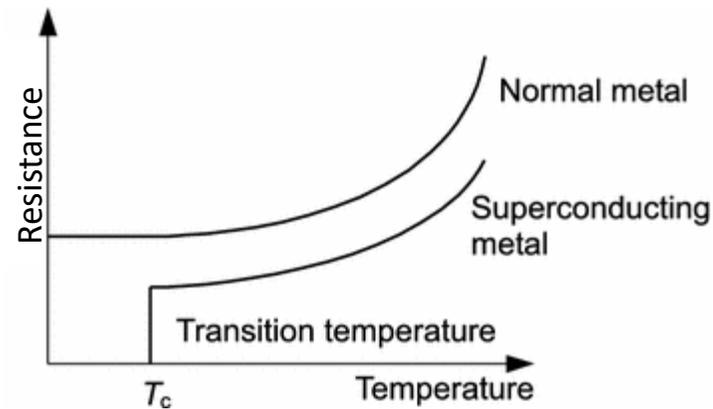
Quantum Materials

- Quantum effects only appear at subatomic sizes, but in certain situations they can have macroscopic effects!



Superconductors

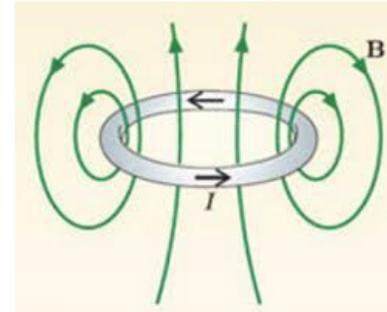
- Certain metals, alloys, and ceramics can conduct electricity with zero electrical resistance when cooled below a certain critical temperature.



- First material discovered to be superconducting was mercury, tin, and lead in 1911 by Kamerlingh Onnes.

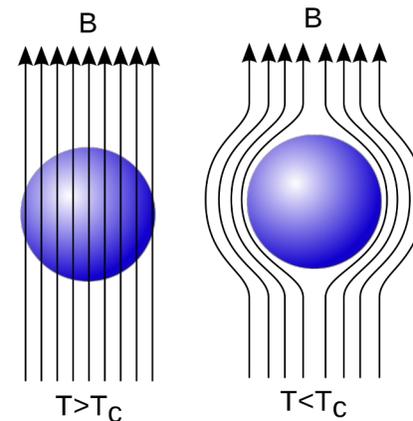
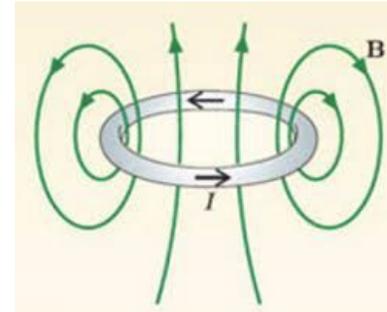
Superconductors

- This behavior can only be explained using quantum physics!
- Electric currents can flow in superconductors without an external voltage



Superconductors

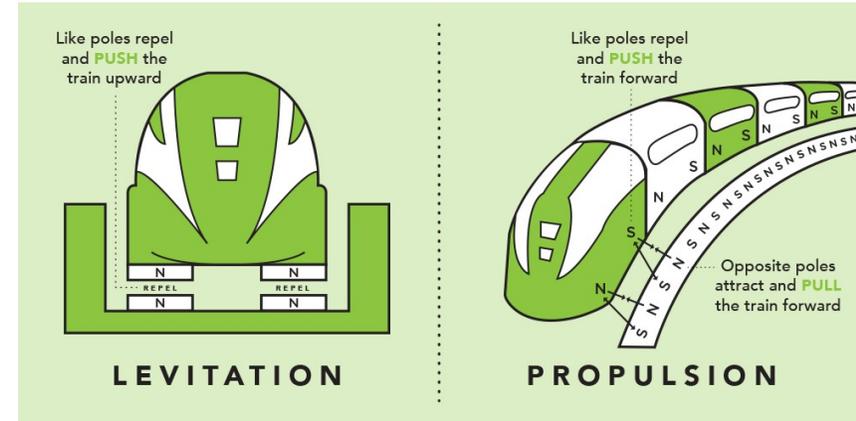
- This behavior can only be explained using quantum physics!
- Electric currents can flow in superconductors without an external voltage
- Superconductors expel magnetic fields (Meissner effect)



Superconductors: Applications

- Very strong superconducting electromagnets

Maglev trains



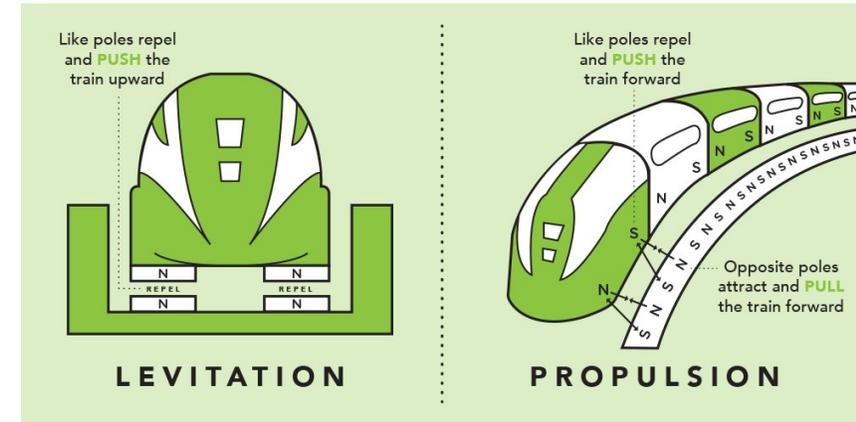
MRI machines



Superconductors: Applications

- Very strong superconducting electromagnets
- Superconducting electric generators and power lines

Maglev trains



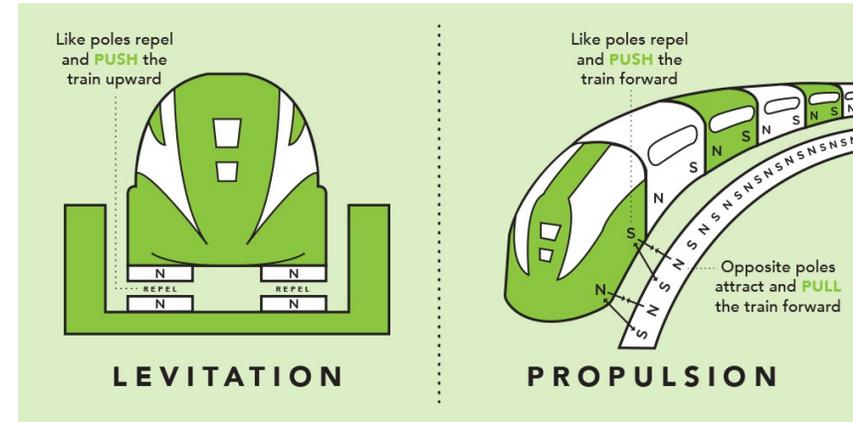
MRI machines



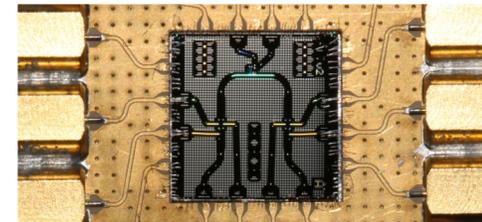
Superconductors: Applications

- Very strong superconducting electromagnets
- Superconducting electric generators and power lines
- Superconducting circuits for quantum computing
- And many more!

Maglev trains

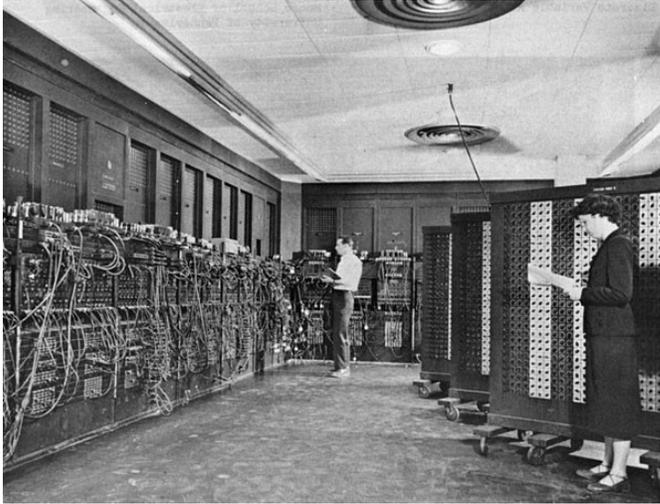


MRI machines



Quantum Computers, Why? (Reason 1)

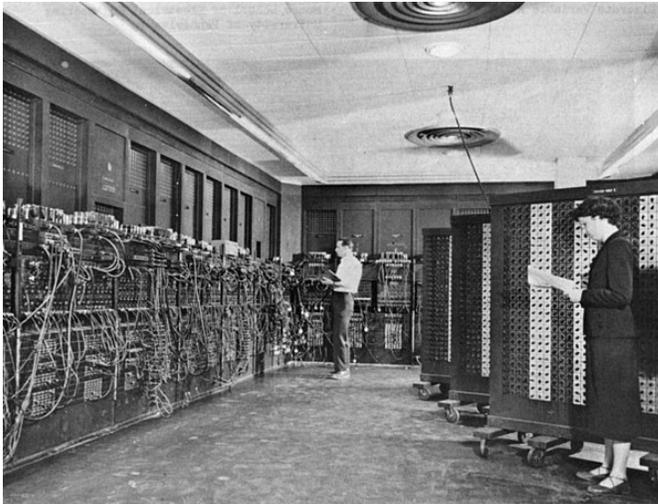
Classical computers have become much smaller as time goes on



1940s

Quantum Computers, Why? (Reason 1)

Classical computers have become much smaller as time goes on



1940s



2020s

How did classical computers become so small?

Quantum Computers, Why? (Reason 1)

Microprocessor



Brain of the computer



Quantum Computers, Why? (Reason 1)

Microprocessor



Brain of the computer

Contains millions of transistors

Putting in more transistors makes your computer faster!



Quantum Computers, Why? (Reason 1)

Microprocessor



Brain of the computer

Contains millions of transistors

Putting in more transistors makes your computer faster!

Problem: Transistors can only become so small...



Quantum Computers, Why? (Reason 1)

Microprocessor



Brain of the computer

Contains millions of transistors

Putting in more transistors makes your computer faster!

Problem: Transistors can only become so small...

For very small objects the laws of physics become governed by quantum physics

A computer based on quantum physics would avoid this problem entirely!

Quantum Computers, Why? (Reason 2)

Nowadays a lot of our personal information is online



Quantum Computers, Why? (Reason 2)

Nowadays a lot of our personal information is online



Online banking

Requires credit card information



How do we protect this information?

Quantum Computers, Why? (Reason 2)

Nowadays a lot of our personal information is online

 Online shopping


BANK OF AMERICA

Online banking

Requires credit card information



How do we protect this information? —> Encryption!

Quantum Computers, Why? (Reason 2)

Nowadays a lot of our personal information is online



Online banking

Requires credit card information



How do we protect this information? —> Encryption!

Encryption works because factorization is very hard for big numbers (for classical computers)

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

35 =

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

$35 = 5 \times 7$ ← Very small number, easy to factorize (thousandths of a second)

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

$35 = 5 \times 7$ ← Very small number, easy to factorize (thousandths of a second)

13123110 =

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

$35 = 5 \times 7$ ← Very small number, easy to factorize (thousandths of a second)

$13123110 = 2 \times 3 \times 5 \times 7 \times 11 \times 13 \times 19 \times 23$ ← Small number, easy to factorize (tenths of a second)

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

$35 = 5 \times 7$ ← Very Small number, easy to factorize (thousandths of a second)

$13123110 = 2 \times 3 \times 5 \times 7 \times 11 \times 13 \times 19 \times 23$ ← Small number, easy to factorize (tenths of a second)

51879984163168498479846518974444408478888406666097984663198410558
88894712364900074066479846413987984634987949649849843111684409849
87662031215947948798465165498748654135498464984611649874984100549
8994874648911116353 =

Quantum Computers, Why? (Reason 2)

What is factorization?

Any whole number is either prime or a product of primes

Primes: 2,3,5,7,11,13,17,19,...

Writing a number as a product of primes is called factorizing

$35 = 5 \times 7$ ← Very Small number, easy to factorize (thousandths of a second)

$13123110 = 2 \times 3 \times 5 \times 7 \times 11 \times 13 \times 19 \times 23$ ← Small number, easy to factorize (tenths of a second)

51879984163168498479846518974444408478888406666097984663198410558

88894712364900074066479846413987984634987949649849843111684409849

87662031215947948798465165498748654135498464984611649874984100549

8994874648911116353 = ? ← Very big number, very hard to factorize

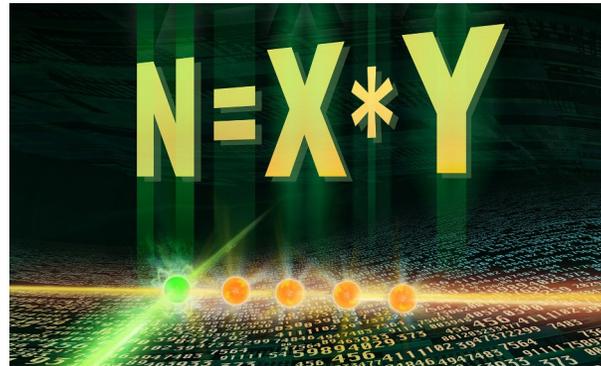
Quantum Computers, Why? (Reason 2)

Quantum computers are much more efficient at factorizing big numbers (Shor's algorithm)



Quantum Computers, Why? (Reason 2)

Quantum computers are much more efficient at factorizing big numbers (Shor's algorithm)

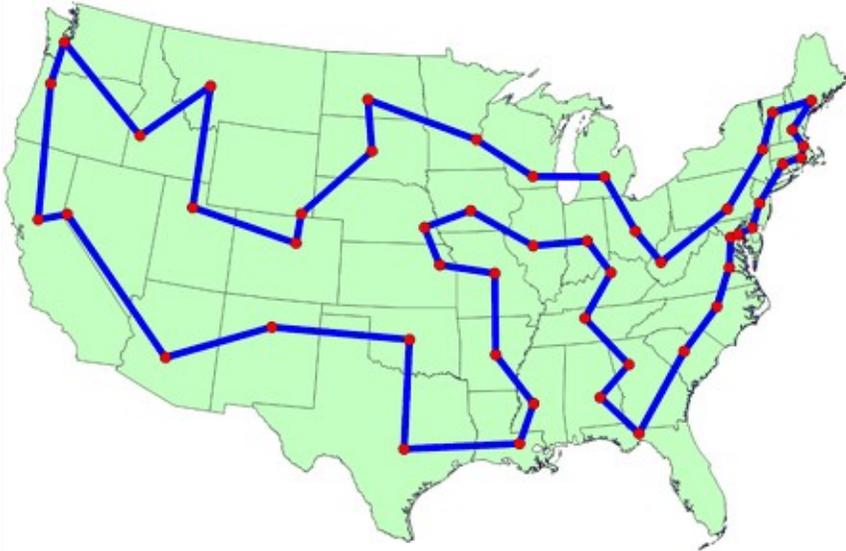


Quantum computers break classical encryption

This can lead to new, more secure, quantum-based encryption methods

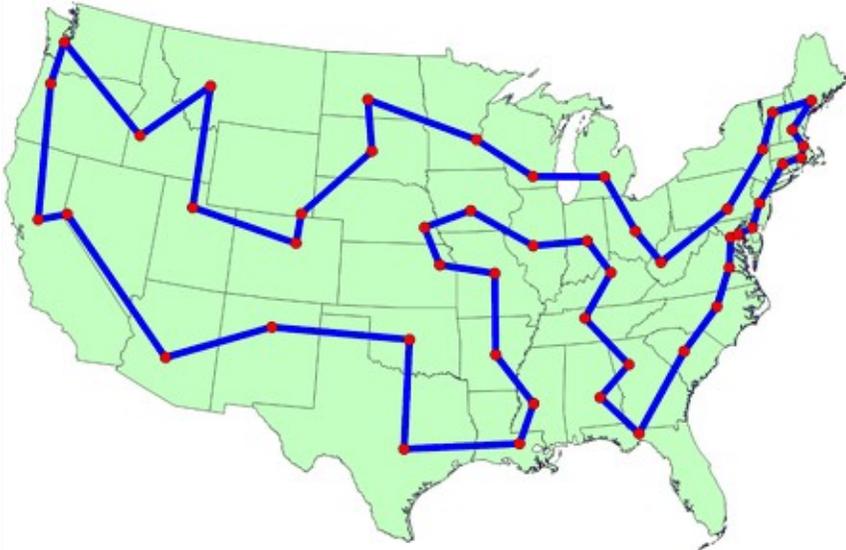
Quantum Computers, Why? (Reason 3)

- Traveling Salesman Problem: given a list of cities, you want to make a round trip that visits each city only once, what is the shortest route?



Quantum Computers, Why? (Reason 3)

- Traveling Salesman Problem: given a list of cities, you want to make a round trip that visits each city only once, what is the shortest route?



Solving this problem has several applications:

- Supply chain logistics
- Commercial flight scheduling
- DNA sequencing
- Designing telecommunication networks
- Etc...

Quantum Computers, Why? (Reason 3)

- A simple way to tackle this problem is to draw all the possible paths, compare them, and then pick the shortest one

Quantum Computers, Why? (Reason 3)

- A simple way to tackle this problem is to draw all the possible paths, compare them, and then pick the shortest one

# of cities	# of paths
2	2
3	6
4	24
5	120
6	720
7	5040
8	40320
9	362880
10	3628800

This method is extremely inefficient!

Quantum Computers, Why? (Reason 3)

- A simple way to tackle this problem is to draw all the possible paths, compare them, and then pick the shortest one

# of cities	# of paths
2	2
3	6
4	24
5	120
6	720
7	5040
8	40320
9	362880
10	3628800

This method is extremely inefficient!

For a large number of cities, it would take the world's most powerful supercomputer millions of years to solve this problem

Quantum Computers, Why? (Reason 3)

- A simple way to tackle this problem is to draw all the possible paths, compare them, and then pick the shortest one

# of cities	# of paths
2	2
3	6
4	24
5	120
6	720
7	5040
8	40320
9	362880
10	3628800

This method is extremely inefficient!

For a large number of cities, it would take the world's most powerful supercomputer millions of years to solve this problem

We need something more than standard computer to try solving this problem!

Break Time!

Take some time to process everything we have seen so far

Welcome Back!

So far we have seen:

- Particle-Wave Duality
- Superposition
- Entanglement
- Superconductors
- Some limitations of classical computers
 - Factorization
 - Traveling Salesman Problem

Enter Quantum Computers

- A quantum computers uses quantum phenomena to process information. They are fundamentally different from classical computers

Enter Quantum Computers

- A quantum computers uses quantum phenomena to process information. They are fundamentally different from classical computers
- Classical computers function using bits
- A bit can only be either 0 or 1

Enter Quantum Computers

- A quantum computers uses quantum phenomena to process information. They are fundamentally different from classical computers
- Classical computers function using bits
- A bit can only be either 0 or 1
- All the data in a classical computer is stored in 0's and 1's, this is called *binary*



What we see



What the computer sees

Enter Quantum Computers

- Quantum computers use quantum bits, known as qubits

Enter Quantum Computers

- Quantum computers use quantum bits, known as qubits
- A qubit can be anywhere between 0 and 1, this is called superposition

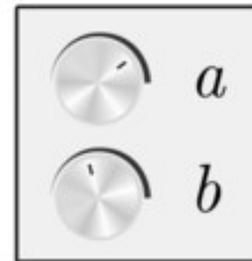
Enter Quantum Computers

- Quantum computers use quantum bits, known as qubits
- A qubit can be anywhere between 0 and 1, this is called superposition

Classical
Bit



Qubit
 $a|0\rangle + b|1\rangle$

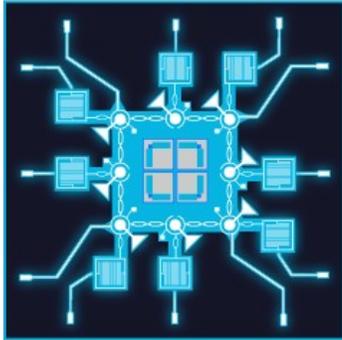


- Qubits can store much more information

Qubits

- There are many different types of qubit

Superconducting Qubits

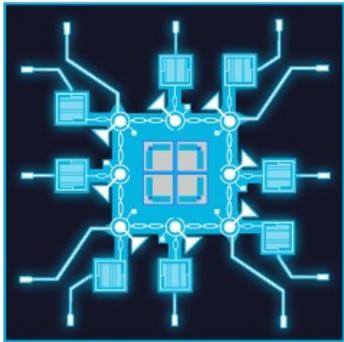


- Fermilab research focuses on superconducting qubits!

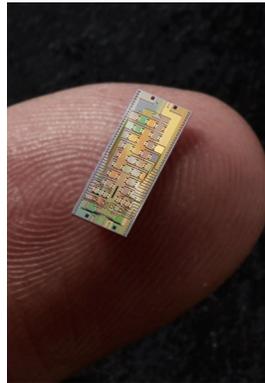
Qubits

- There are many different types of qubit

Superconducting Qubits



Photonic Qubits

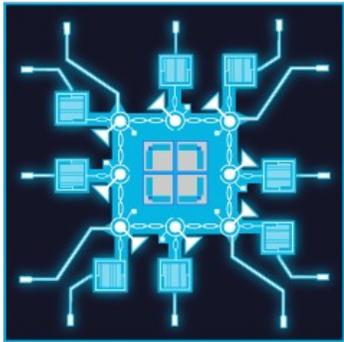


- Fermilab research focuses on superconducting qubits!

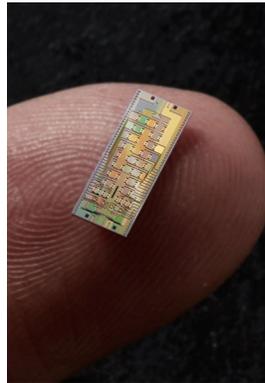
Qubits

- There are many different types of qubit

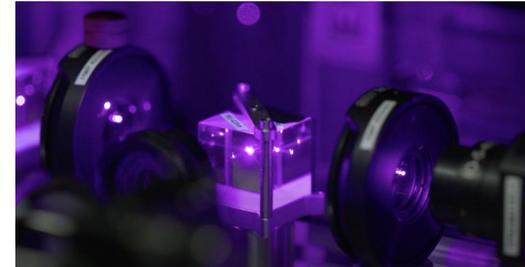
Superconducting Qubits



Photonic Qubits



Rydberg Atom Qubits



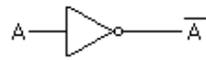
- Fermilab research focuses on superconducting qubits!

Logic Circuits

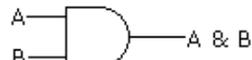
- How do computers process information?

Logic Circuits

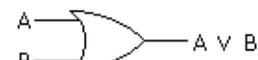
- How do computers process information?
- Logic gates are the basic building blocks of classical computers



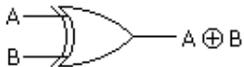
A	NOT A
0	1
1	0



A	B	A AND B
0	0	0
0	1	0
1	0	0
1	1	1



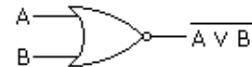
A	B	A OR B
0	0	0
0	1	1
1	0	1
1	1	1



A	B	A XOR B
0	0	0
0	1	1
1	0	1
1	1	0



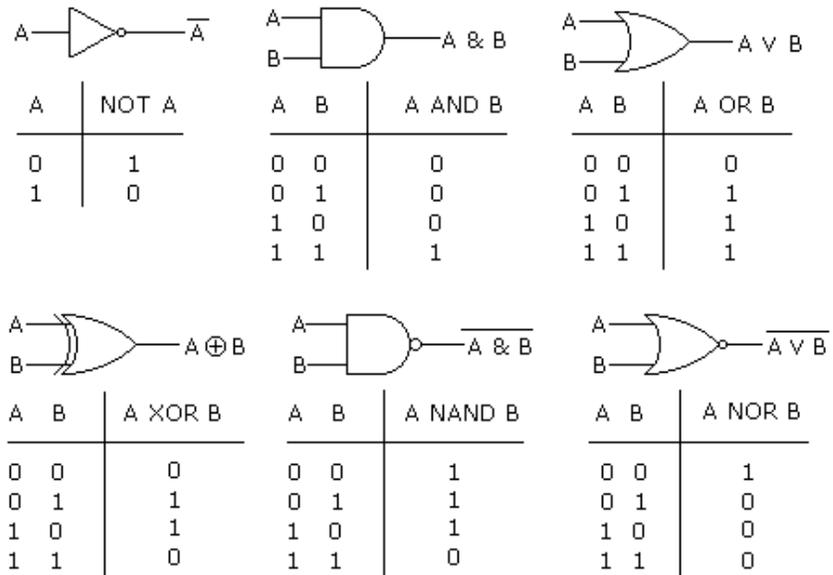
A	B	A NAND B
0	0	1
0	1	1
1	0	1
1	1	0



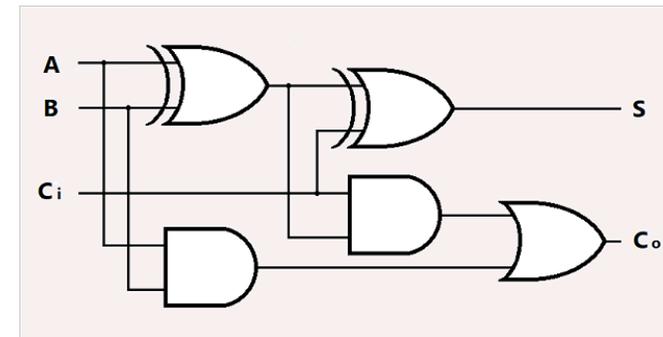
A	B	A NOR B
0	0	1
0	1	0
1	0	0
1	1	0

Logic Circuits

- How do computers process information?
- Logic gates are the basic building blocks of classical computers



Connecting many logic gates together makes a logic circuit



A standard CPU contains millions of logic gates

Quantum Circuits

- Quantum gates are the basic building blocks of quantum computers

X Gate
 Bit-flip, Not

$$\begin{array}{c} \boxed{X} \\ \equiv \\ \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} \\ = \\ \beta|0\rangle + \alpha|1\rangle \end{array}$$

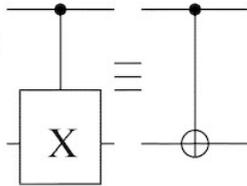
Z Gate
 Phase-flip

$$\begin{array}{c} \boxed{Z} \\ \equiv \\ \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} \\ = \\ \alpha|0\rangle - \beta|1\rangle \end{array}$$

H Gate
 Hadamard

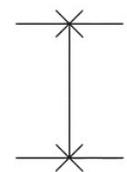
$$\begin{array}{c} \boxed{H} \\ \equiv \\ \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} \\ = \\ \frac{\alpha + \beta|0\rangle + \alpha - \beta|1\rangle}{\sqrt{2}} \end{array}$$

Controlled Not
 Controlled X
 CNot



$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + b|01\rangle + d|10\rangle + c|11\rangle$$

Swap



$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + c|01\rangle + b|10\rangle + d|11\rangle$$

Quantum Circuits

- Quantum gates are the basic building blocks of quantum computers

X Gate
Bit-flip, Not

$$\begin{array}{|c} \hline \text{X} \\ \hline \end{array} \equiv \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \beta|0\rangle + \alpha|1\rangle$$

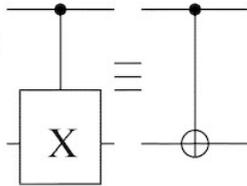
Z Gate
Phase-flip

$$\begin{array}{|c} \hline \text{Z} \\ \hline \end{array} \equiv \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \alpha|0\rangle - \beta|1\rangle$$

H Gate
Hadamard

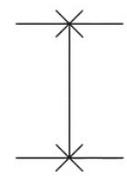
$$\begin{array}{|c} \hline \text{H} \\ \hline \end{array} \equiv \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \frac{\alpha + \beta|0\rangle + \alpha - \beta|1\rangle}{\sqrt{2}}$$

Controlled Not
Controlled X
CNot



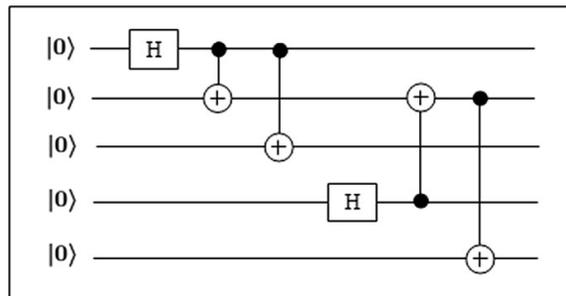
$$\equiv \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + b|01\rangle + d|10\rangle + c|11\rangle$$

Swap



$$\equiv \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = a|00\rangle + c|01\rangle + b|10\rangle + d|11\rangle$$

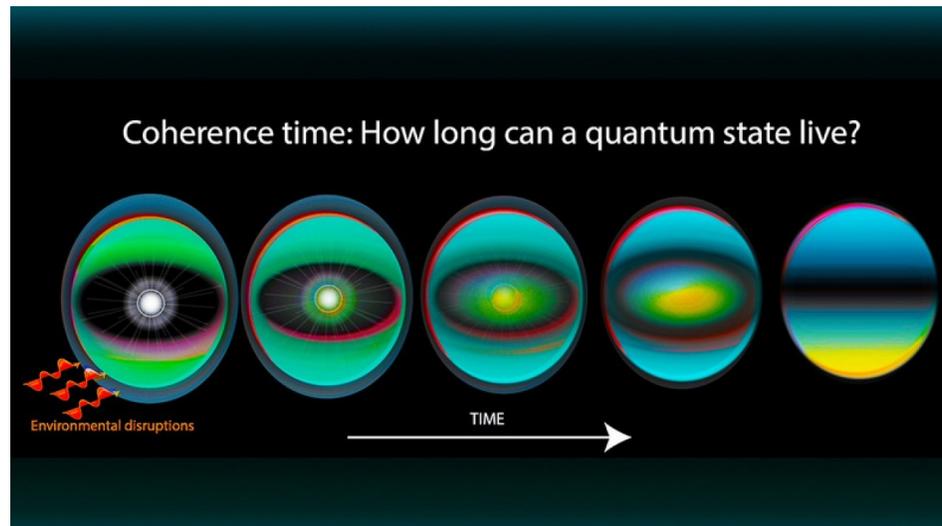
- Quantum gates act on a qubit of the form $\alpha|0\rangle + \beta|1\rangle$



Putting many quantum gates together creates a quantum circuit

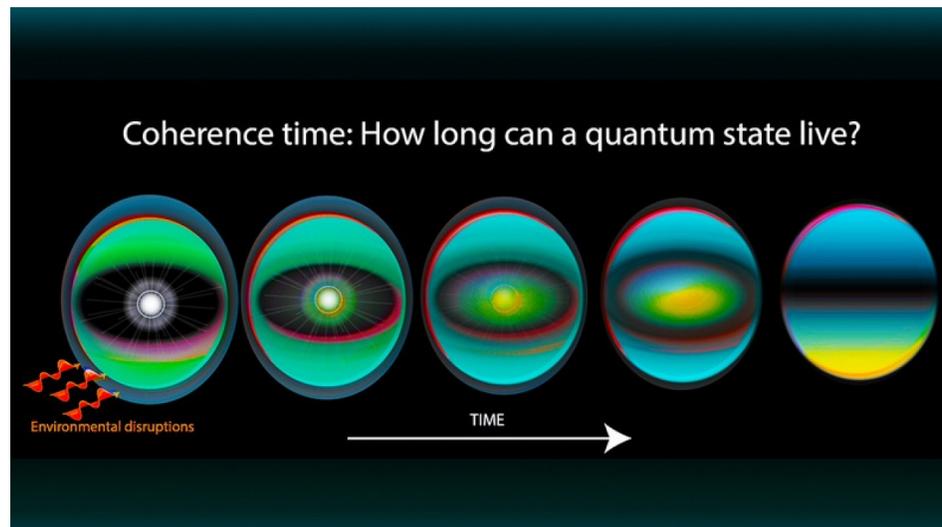
Obstacles

- Qubits are very sensitive to external disruptions and really difficult to handle. This is called decoherence.



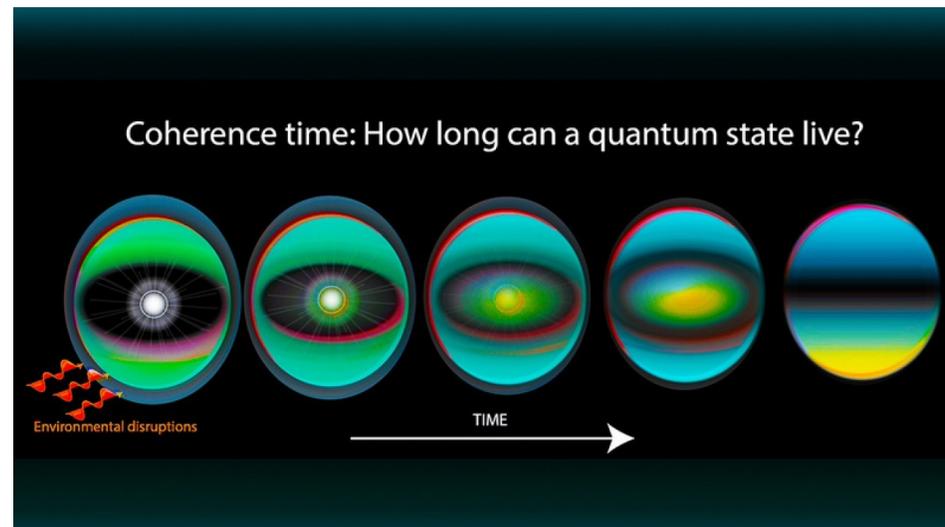
Obstacles

- Qubits are very sensitive to external disruptions and really difficult to handle. This is called decoherence.
- Requires extreme conditions (temperatures of around -459°F)



Obstacles

- Qubits are very sensitive to external disruptions and really difficult to handle. This is called decoherence.
- Requires extreme conditions (temperatures of around -459°F)
- Scaling (can only control a few qubits at a time)

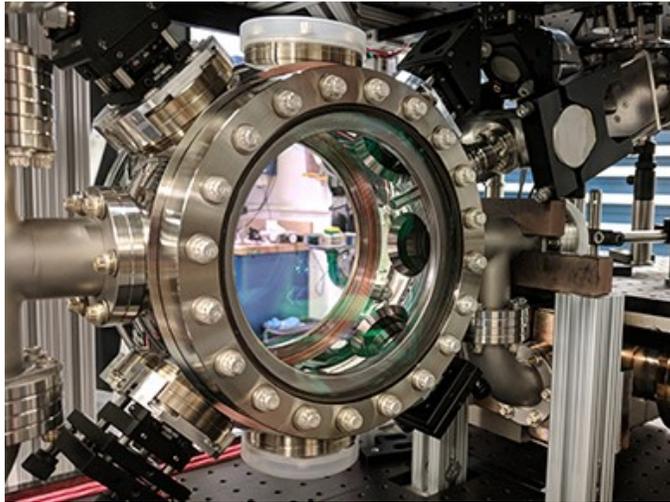


Quantum Sensors

- The extreme sensitivity of qubits can be used to create very precise detection devices

Quantum Sensors

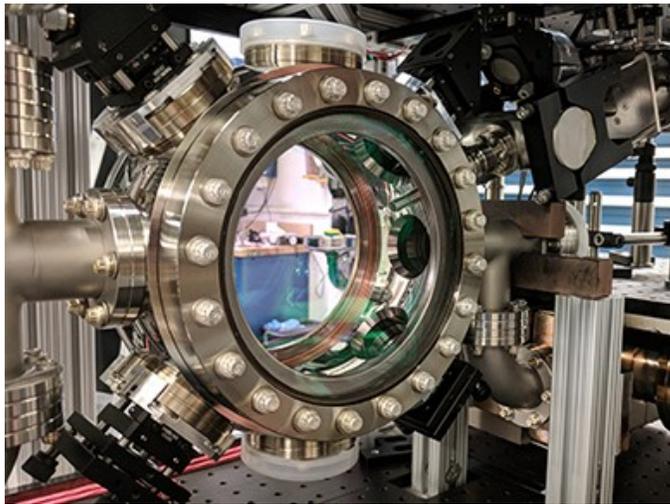
- The extreme sensitivity of qubits can be used to create very precise detection devices
- Quantum sensors beat the performance of any classical sensor technology



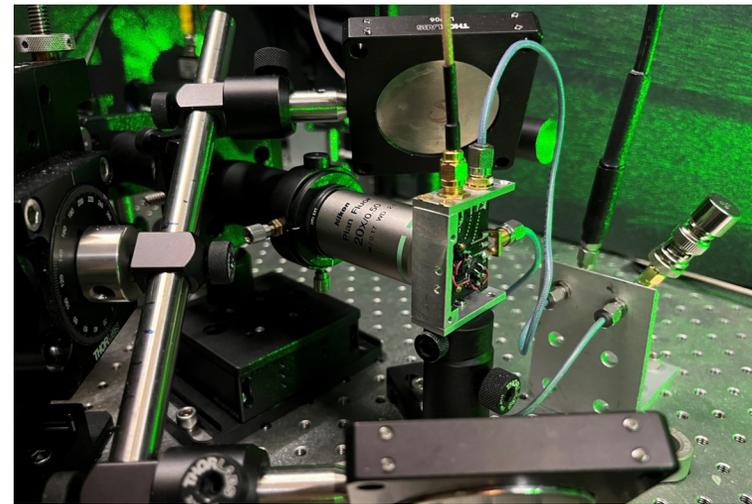
MAGIS-100 (Fermilab)

Quantum Sensors

- The extreme sensitivity of qubits can be used to create very precise detection devices
- Quantum sensors beat the performance of any classical sensor technology



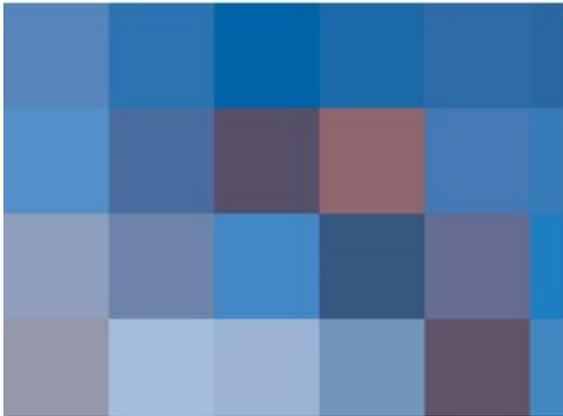
MAGIS-100 (Fermilab)



Quantum Sensor (MIT)

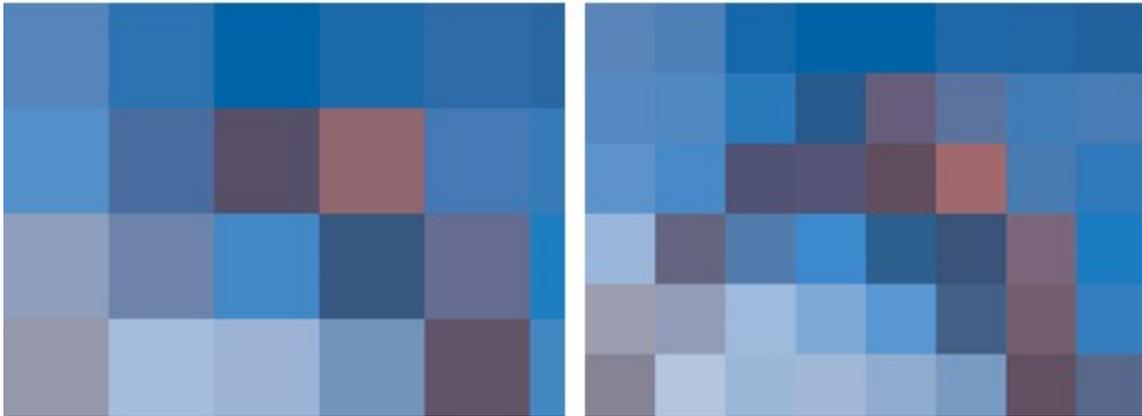
Quantum Sensors

- What do we want high precision for?



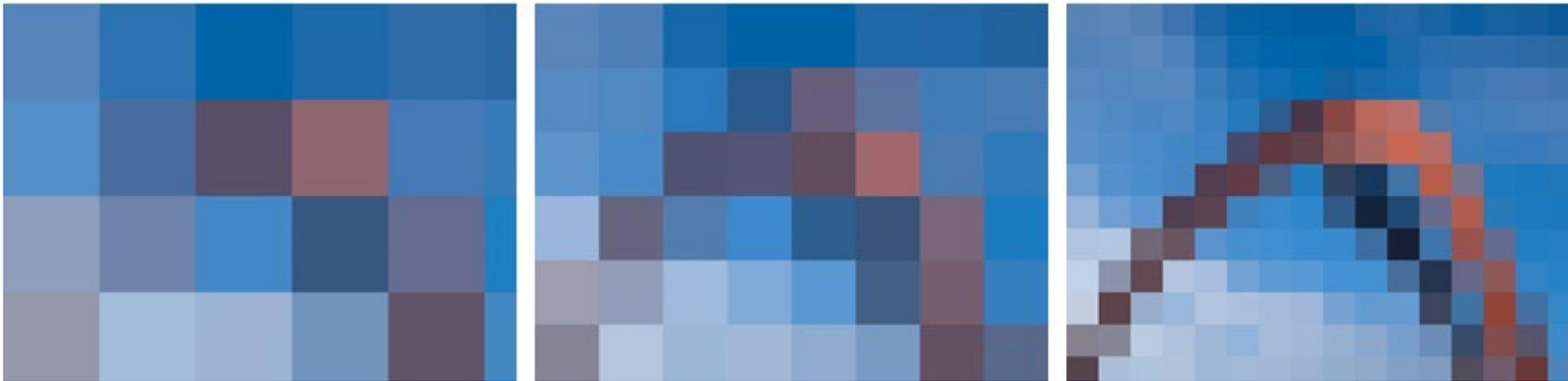
Quantum Sensors

- What do we want high precision for?



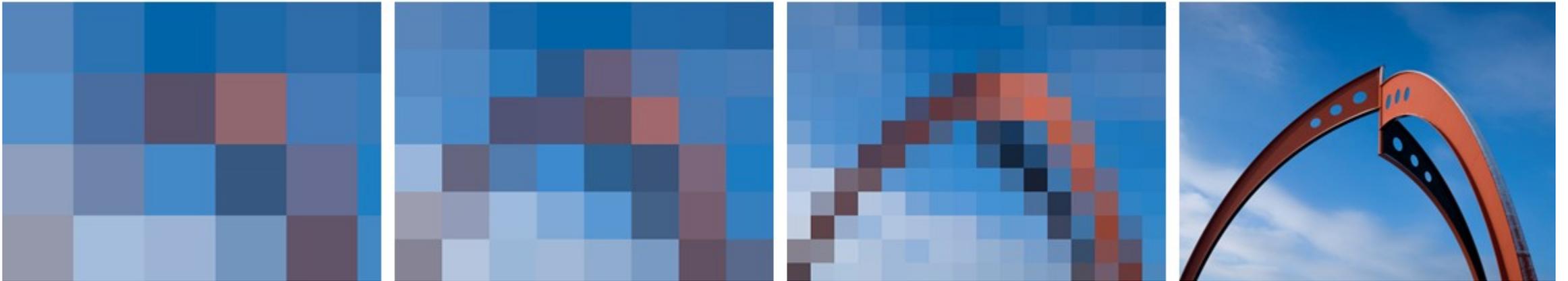
Quantum Sensors

- What do we want high precision for?



Quantum Sensors

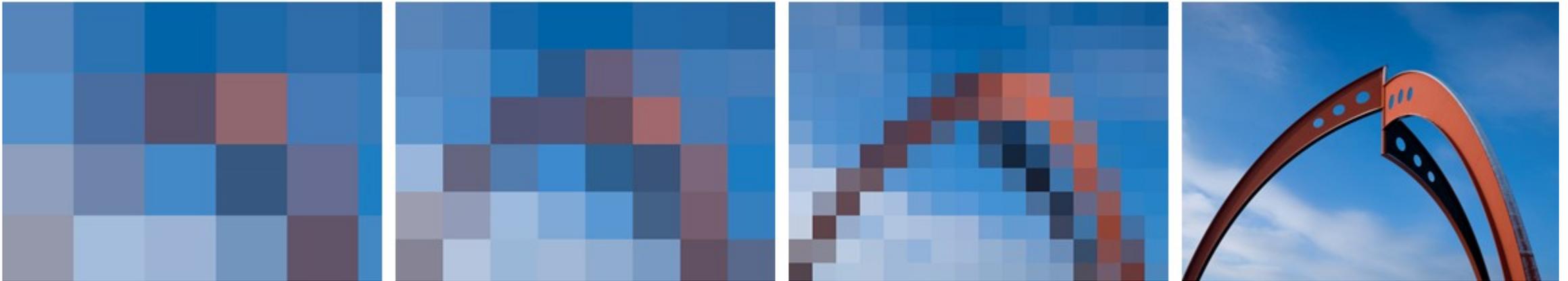
- What do we want high precision for?



- As precision increases new features are discovered.

Quantum Sensors

- What do we want high precision for?



- As precision increases new features are discovered.

- Chemistry example: sodium doublet. →



Quantum Sensors

- Quantum sensors use entangled states to overcome limitations of classical sensors

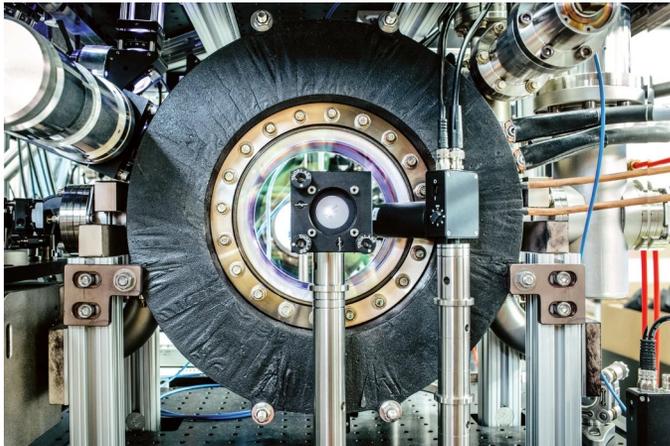
Quantum Sensors

- Quantum sensors use entangled states to overcome limitations of classical sensors
- What can we do with this increased precision/sensitivity?

Quantum Sensors

- Quantum sensors use entangled states to overcome limitations of classical sensors
- What can we do with this increased precision/sensitivity?

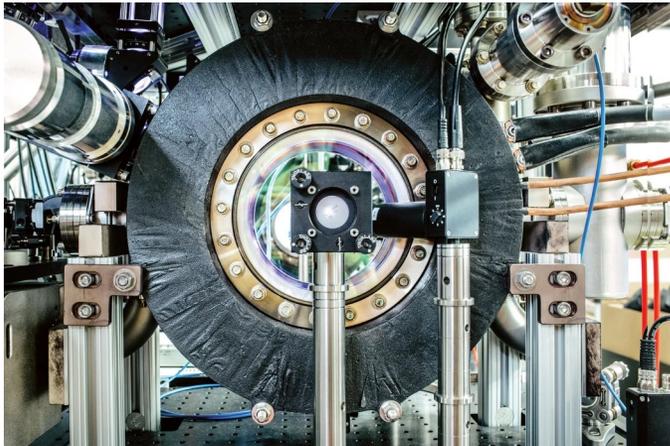
Gravitational
wave detection



Quantum Sensors

- Quantum sensors use entangled states to overcome limitations of classical sensors
- What can we do with this increased precision/sensitivity?

Gravitational
wave detection



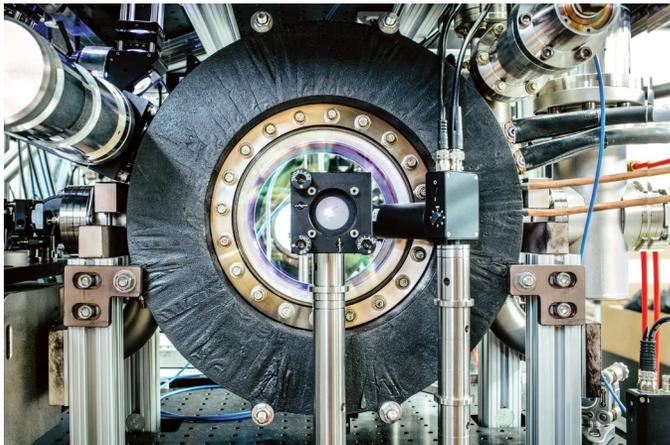
Dark matter
detection



Quantum Sensors

- Quantum sensors use entangled states to overcome limitations of classical sensors
- What can we do with this increased precision/sensitivity?

Gravitational
wave detection



Dark matter
detection



Medical imaging

